

Ex 14 Une suite arithmétique.

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Tous les 5 termes, la suite se répète.

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$$\text{Donc } a_{2014} = a_{4+2010} = a_4 = \mathbf{1/8}.$$